

Section 3.8

Example: The position of a particle is given by the equation $s = f(t) = t^3 - 6t^2 + 9t$ where t is measured in seconds and s in meters.

a) Find the velocity at time t .

$$v(t) = 3t^2 - 12t + 9$$

b) What is the velocity after 2 s? After 4 s?

$$v(2) = -3 \text{ m/s}$$

$$v(4) = 9 \text{ m/s}$$

c) When is the particle at rest?

$$v(t) = 0 \quad \text{so} \quad 3(t^2 - 4t + 3) = 0$$

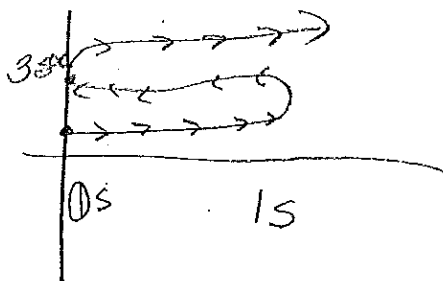
$$\text{at } 1 \text{ s \& } 3 \text{ s} \quad 3(t-3)(t-1) = 0$$

d) When is the particle moving forward?

$$v(t) = + \quad \begin{array}{l} t-3 > 0 \quad t-1 > 0 \\ t > 3 \quad t > 1 \end{array}$$

$(3, \infty)$ moving forward
 $(0, 1)$

e) Draw a diagram to represent the motion of the particle.



- f) Find the total distance traveled by the particle during the first five seconds.

$$\begin{aligned} s(1) - s(0) &= 4 - 0 \\ s(3) - s(1) &= 0 - 4 \\ s(5) - s(3) &= 20 - 0 \end{aligned} \quad \left. \vphantom{\begin{aligned} s(1) - s(0) \\ s(3) - s(1) \\ s(5) - s(3) \end{aligned}} \right\} + 28 \text{ m}$$

- g) Find the acceleration at time t and after 4 s.

$$\begin{aligned} 6t - 12 &= a(t) \\ a(4) &= 12 \text{ m/s}^2 \end{aligned}$$

- h) On your calculator, graph s , v , and a using the window $x = [0, 5]$ scale of 1, $y = [-15, 25]$ scale of 5.

When the velocity and the acceleration are either both positive or both negative, the particle is speeding up. When v and a have opposite signs, the particle is slowing down.

- i) When is the particle speeding up? Slowing down?

$$\begin{aligned} a(t) = 6t - 12 > 0 & \text{ when } t > 2 & + (2, \infty) \\ 6t - 12 < 0 & \text{ when } t < 2 & - (0, 2) \end{aligned}$$

so su $(1, 2)$ $(3, \infty)$

sd $(0, 1)$ $(2, 3)$

237 $(1, 5-7)$

Section 3.8 day 2

Cost Function: the total cost a company incurs in producing x units of a certain commodity defined by $f(x)$.

Marginal Cost: the instantaneous rate of change in cost with respect to the number of items produced. (the derivative).

Example: A company produces baseball caps and estimates the cost of producing x baseball caps is

$$C(x) = 10,000 + 5x + 0.01x^2.$$

- Find the marginal cost function
- Find $C'(500)$ and explain what it means. What does it predict?
- Compare $C'(500)$ with the cost of manufacturing the 501st cap.

a) $C'(x) = 5 + .02x$

b) $C'(500) = 5 + .02(500) = \$1.5/\text{cap}$ - rate \$ is increasing with respect to x when $x = 500$ predicts the 501st cap cost.

c) $C(501) - C(500) = \$15.01$
 $15015.01 - 15000$

8, 9, 11, 13_{ab}, 14, 15, 18, 29, 30

Homework: page 210 #6, 7, 9, 11ab, 12, 16, 27, 28