

Sec 2.1 page 94 (1ab, 3, 6-8)

$$\textcircled{1} a) t=5 \quad M_{pg} = \frac{250 - 694}{15 - 5} = \boxed{-44.4 \text{ g/min}}$$

$$t=10 \quad M_{pg} = \frac{250 - 444}{15 - 10} = \boxed{-38.8 \text{ g/min}}$$

$$t=20 \quad M_{pg} = \frac{250 - 111}{15 - 20} = \boxed{-27.8 \text{ g/min}}$$

$$t=25 \quad M_{pg} = \frac{250 - 28}{15 - 25} = \boxed{-22.2 \text{ g/min}}$$

$$t=30 \quad M_{pg} = \frac{250 - 0}{15 - 30} = \boxed{-16.67 \text{ g/min}}$$

$$b) \text{ using } t=10 \text{ + } t=20 \text{ we have } \frac{-38.8 + -27.8}{2} = \boxed{-33.3 \text{ g/min}}$$

$$\textcircled{3} a) i) = 0.333333$$

$$ii) = 0.263158$$

$$iii) = 0.251256$$

$$iv) = 0.250125$$

$$v) = 0.2$$

$$vi) = 0.238095$$

$$vii) = 0.248756$$

$$viii) = 0.249875$$

b) The slope appears to be $\frac{1}{4}$.

$$c) y - \frac{1}{2} = \frac{1}{4}(x - 1)$$

$$\text{or } y = \frac{x}{4} + \frac{1}{4}$$

$$m = \frac{y - y_1}{x - x_1}$$

$$m(x - x_1) = y - y_1$$

$$y - y_1 = m(x - x_1)$$

$$(1, \frac{1}{2}) \quad m = \frac{1}{4}$$

$$y - \frac{1}{2} = \frac{1}{4}(x - 1)$$

$$(6) a) t=1 \quad y=8.14 \Rightarrow (1, 8.14)$$

V_{ave} between 1 and $1+h$ can be found by the equation

$$V_{ave} = \frac{y(1+h) - y(1)}{(1+h) - 1} = \frac{10(1+h) - 1.86(1+h)^2 - 8.14}{h}$$
$$= \frac{10 + 10h - 1.86 - 3.72h - 1.86h^2 - 8.14}{h}$$
$$= \frac{6.28h - 1.86h^2}{h} = \boxed{6.28 - 1.86h}$$

i) $h=1$ $V_{ave} = 4.42 \text{ m/s}$
ii) $h=.5$ $V_{ave} = 5.35 \text{ m/s}$
iii) $h=.1$ $V_{ave} = 6.094 \text{ m/s}$
iv) $h=.01$ $V_{ave} = 6.2614 \text{ m/s}$
v) $h=.001$ $V_{ave} = 6.27814 \text{ m/s}$

$$b) V(1) = \boxed{6.28 \text{ m/s}}$$

$$(7) i) = \frac{10.7 - 1.4}{3 - 1} = 4.65 \text{ m/s}$$

$$ii) 5.6 \text{ m/s}$$

$$iii) 7.55 \text{ m/s}$$

$$iv) 7 \text{ m/s}$$

b) I used the points (2, 4) and (5, 23) as they appear to make a good tangent line at $t=3$.

$$\therefore \frac{23 - 4}{5 - 2} \approx 6.3 \text{ m/s}$$

$$\textcircled{8} \text{ a) } \frac{S_2 - S_1}{2 - 1} = \frac{3 - -3}{1} = 6 \text{ cm/s}$$

$$\text{ii) } V_{ave} = -4.71 \text{ cm/s}$$

$$\text{iii) } V_{ave} = -6.13 \text{ cm/s}$$

$$\text{iv) } V_{ave} = -6.27 \text{ cm/s}$$

$$\text{b) } V(s) \approx -6.3 \text{ cm/s}$$